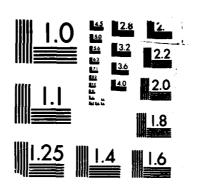
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A CRITICAL SPEED STUDY FOR **AIRCRAFT BIAS PLY TIRES**



J.H. Champion P.M. Wagner Launch and Recovery Branch **Vehicle Subsystems Division**

January 1988

Final Report for Period October 1986 - August 1987

Approved for public release; distribution unlimited.



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Joseph P. Fellner

Power Technology Branch Aerospace Power Division Aero Propulsion Laboratory Batteries and Fuel Cells Power Technology Branch Aerospace Power Division

FOR THE COMMANDER

JAMES D. REAMS

Chief, Aerospace Power Division

Aero Propulsion Laboratory

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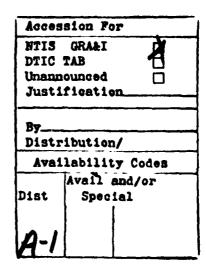
SUMMARY

The governing differential equation describing the vertical motion of the tire tread band as a straight beam on an elastic foundation, under tension, is derived. An assumed mode wave solution is used to derive the critical speed equation from the governing differential equation. The effective tire structural properties used in the critical speed equation are the tread band bending stiffness (EI), the elastic foundation linear spring constant (k), the belt tension due to inflation pressure (T_p) , and the tread band effective density (ρ') . These relations are presented as equations 2-21, 2-22, 2-27, and 2-40.

A parametric study is presented, describing the influence of tire inflation pressure, cord half angle, loaded vertical deflection, tread depth, and aspect ratio on critical speed. Those parameters affecting the bending stiffness and tread band tension have the greatest influence on critical speed. These parameters are the cord half angle, tread depth, tire inflation pressure, and aspect ratio. The tire vertical deflection has the least influence on critical speed for a given inflation pressure.

Dynamometer tests of a 49x17/26PR Type VII Goodyear tire were conducted to validate the predicted trends of critical speed versus tire inflation pressure, tread depth, and loaded vertical deflection. Results to date have indicated that the critical speed model has correctly predicted trends. Predicted critical speed values have ranged from -1.5 percent to +13.3 percent error with an average of 2.9 percent error.





FOREWORD

This report documents the work during an effort to develop and validate a critical speed prediction model defining the linear speed at which the onset of a standing wave occurs in the tread band of high speed aircraft bias tires. The work was performed by the Launch and Recovery Branch, Vehicle Subsystems Division, Flight Dynamics Laboratory, Air Force Wright Aeronautical Laboratories, Wright-Patterson Air Force Base, Ohio, between October 1986 and August 1987. The project, task, and work unit numbers are 2402, 240201, and 24020150, respectively.

The authors wish to express appreciation to Dr Samuel K. Clark of the Precision Measurement Company for his technical assistance.

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SECTION I

INTRODUCTION

BACKGROUND

The trend in aircraft and aerospace vehicle design is toward high wing loaded vehicles. This trend is especially evident in the advanced aerospace vehicle concepts currently under study by the Air Force and NASA. Examples of these advanced aerospace vehicle concepts are the National Aerospace Plane and the Objective Vehicle of the Air Force Advanced Launch System Technology Program. Whether having the capability to takeoff, land, or both, in a conventional horizontal fashion, the load and speed requirements of the advanced aerospace vehicle concepts are expected to exceed current state of the art in landing gear performance. One such deficiency involves the upper speed and load limits of current high performance tires. This deficiency is exemplified by the extreme wear problems associated with the Space Shuttle's main landing gear tires during a single landing. The wear is so severe during the first few seconds of touchdown that the tires have been dubbed "half landing tires".

A tire's performance can be measured by its durability, the ability to repeatedly function at design conditions. Aside from wear limits, a tire's long and short term durability may be characterized by its structural integrity. Long term durability may be defined as the tire's ability to retain structural integrity (i.e., carcass/rubber adhesive strength) over a history of stress/temperature cycles typical of its operational use. Short term durability may be defined as the tire's ability to survive at its upper performance limits of speed and load. The critical speed is the tire's upper speed capability characterized by its structural limits such as loss of cohesive and adhesive tread retention due to centrifugal effects or the destructive mechanical deformation of the standing wave. The critical speed can be a measure of the tire's short term durability.

This report presents results of an Air Force study investigating critical speed as a function of the standing wave phenomenon in the tread band region of bias ply aircraft tires.

OBJECTIVE

The purpose of this study is to develop a simple closed-form solution that will correctly describe the trends of a bias tire's critical speed as a function of its design and operational characteristics. Critical speed is defined as the velocity at which a standing wave develops in the tread band. The standing wave is represented by a sinusoidal deformation of the tread band around the circumference of the tire. The standing wave is first apparent as the tread elements roll out of the tire footprint. This creates a stress concentration, and in turn, rapid heat generation that may lead to structural failure if critical speed is maintained or exceeded. If the critical speed of bias tires is successfully predicted analytically, then the resulting critical speed model will be used as a tool for the design and assessment of tire designs for application to advanced aerospace vehicles.

APPROACH

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A simple closed-form solution described as the critical speed equation was developed as a first-cut prediction tool. Several high-speed tires were selected to conduct critical speed dynamometer tests as a function of tire inflation pressure, tire tread depth, and tire deflection. To date, only a small number of tests have been completed on one tire size, the 49x17/26PR Type VII Goodyear tire. The unvalidated critical speed equation was used to generate an initial test matrix. It was assumed that the critical speed equation was capable of correctly predicting critical speed for a set of test conditions within a band of plus or minus 20 percent. The tires were tested at constant speed, starting at the lower end of the speed band. The test speed was increased from one test cycle to the next until the standing wave was detected visually. Results of the dynamometer tests will be used to make refinements if necessary to both the model and test methodology.

SECTION II

THEORY

This section describes the development of the critical speed equation. The governing differential equation from which the critical speed equation is derived describes the oscillatory motion of a straight beam on an elastic foundation, and is considered to be a reasonable representation of the tread band for a bias ply tire subject to the standing wave phenomenon [2][3]. Derivation of the governing differential equation is first described, followed by its solution representing the critical speed associated with the standing wave. Descriptions of the constitutive equations defining the terms of the critical speed equation are also discussed.

DERIVATION OF THE GOVERNING DIFFERENTIAL EQUATION

The variational method is used to derive the governing differential equation. First consider the principle of virtual work which is stated as follows:

"A necessary and sufficient condition for the equilibrium of a system of particles or a continuum system is that the work done by the external forces acting upon the system plus the work done by the internal forces of the system must vanish for any virtual displacement." [1]

Virtual displacements are fictitious motions which are assumed to occur with the actual forces remaining constant. Virtual displacement must be kinematically admissible, (i.e., they can not violate the physical restraints of the system). Virtual work is that work performed during virtual displacements. The principle of virtual work can be expressed as

$$\delta W_e = -\delta W_i \tag{2-1}$$

where,

 δW_e = virtual work performed by external forces

 $\delta W_i = \text{virtual work performed by internal forces}$

If the external and internal forces are considered conservative, then the first-order variation of the potential energy of the internal forces and external forces can be related to virtual work as follows:

$$\delta W_{\epsilon} = -\delta V \tag{2-2}$$

$$\delta W_i = -\delta U \tag{2-3}$$

where,

U = Internal potential energy

V = external potential energy.

The principle of the stationary value of the total potential can be derived by combining equations (2-1) through (2-3) and expressed symbolically as

$$\delta(U+V)=0 \tag{2-4}$$

where,

THE SOUND PROPERTY OF THE SOUND STATES OF THE

$$U + V = \text{total potential}$$

The principle of stationary value of the total potential may be stated as:

"A necessary and sufficient condition for the equilibrium of conservative forces acting on a system of particles or a continuum is that the first-order variation of the total potential must vanish for any virtual displacement [1]."

Before taking the first-order variation (b) and applying the above stated principle, the internal potential energy (U) and external potential energy (V) must be defined for the system of interest. The system under consideration is a straight beam on an elastic foundation under tension, see Figure 1. Only those terms containing the vertical deflection (w) and its derivatives (i.e., $w' = \partial w/\partial x$) are of interest for this study, and only those terms will be retained in the potential energy equations. The vertical displacement of the beam corresponds to the radial (outward) displacement of the tire tread band.

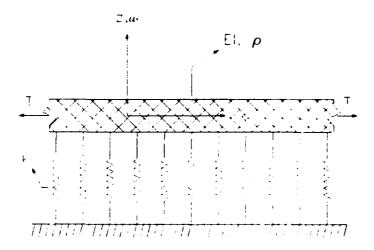


Figure 1. Straight Beam On an Elastic Foundation

The strain energy (U_{se}) contributes to the internal potential energy (U). Although the behavior of tire materials is nonlinear, when determining the onset of the standing wave it is

reasonable to assume linear material properties. Assuming that all stress components other than σ_{xx} , are negligible, and that the material is linear and elastic ($\sigma_{xx} = E\epsilon_{xx}$), the strain energy over an element volume is defined as

$$U_{se} = \int_{V} \left[\int \sigma_{xx} d\epsilon_{xx} \right] dV$$
$$= \int_{V} \left[\int \left(\frac{\sigma_{xx}}{E} \right) d\sigma_{xx} \right] dV$$
$$= \frac{1}{2E} \int_{V} \sigma_{xx}^{2} dV.$$

The component of σ_{xx} in terms of w and/or its derivatives for a beam in bending is simply $\sigma_{xx} = -Ezw''$. Substituting this relation for σ_{xx} and assuming a beam of unit width gives

$$U_{se} = \frac{1}{2} \int_0^L EI(w'')^2 dx \qquad (2-5)$$

where,

L = length of the beam.

The elastic foundation provides an additional term to the internal potential energy. The elastic restraints (i.e., combined effect of tire internal inflation pressure and tire sidewall) are assumed to be evenly distributed over the length of the beam and defined by a linear spring constant k, relating a force per unit area (P) to vertical displacement (w). The internal energy due to the elastic foundation is defined as

$$U_{ef} = \int_{0}^{L} \int_{0}^{W} P dw dx$$
$$= \frac{1}{2} \int_{0}^{L} kw^{2} dx \qquad (2-6)$$

The net internal energy is the superposition of U_{se} and U_{ef} , and is defined as

$$U = U_{se} + U_{ef}$$

$$= \frac{1}{2} \int_0^L \left[EI(w'')^2 + kw^2 \right] dx. \qquad (2-7)$$

The external potential energy has a contribution in terms of w due to the tension force T. This contribution comes about because the point of application of the force T is free to move in the x-direction as bending occurs, and is defined as

$$V_T = T\Delta(x)$$

where,

$$\Delta(x) = \frac{1}{2} \int_0^L (w')^2 dx$$

which is obtained from retaining the first term in the binomial expansion of

$$\Delta(x) = \int_0^L \left[\sqrt{dx^2 + dw^2} - dx \right]$$

Any distribution load q(x) also produces a contribution to the external potential energy V in the form of

 $V_d = -\int_0^L q(x)wdx.$

The net external energy becomes

$$V = V_T + V_d$$

$$= \int_0^L \left[\frac{T(w')^2}{2} - q(x)w \right] dx.$$
 (2-8)

The total potential (U+V) is found from equations 2-7 and 2-8, giving

$$U+V=\frac{1}{2}\int_0^L \left[EI(w'')^2+T(w')^2+kw^2-qw\right]dx. \qquad (2-9)$$

The principle of stationary value of the total potential can now be applied. As a result of the applied loads, the beam will assume an equilibrium state described by w(x). Taking the first-order variation of the total potential (equations 2-4 and 2-9) gives

$$\int_0^L EIw''\delta w''dx + \int_0^L kw\delta wdx + T\int_0^L w'\delta w'dx - \int_0^L q\delta wdx = 0.$$

Integrating by parts the first and third terms leads to the following expanded form,

$$EI \left[\delta w'(L) - \delta w'(0) \right] w'' - EI \left[\delta w(L) - \delta w(0) \right] w'' + \int_0^L EI(w'')'' \delta w dx \\ - \int_0^L q \delta w dx + \int_0^L kw \delta w dx + Tw' \left[\delta w(L) - \delta w(0) \right] - T \int_0^L \delta w w'' dx = 0.$$

If the structure of interest is a tire tread band which closes upon itself with circumference equal to beam length L, it can be imagined that x=0 corresponds to x=L. Therefore, $\delta w(0)$ must equal $\delta w(L)$ and $\delta w'(0)$ must equal $\delta w'(L)$. The first-order variation of the total potential reduces to

$$\int_0^L \left[EI(w'')'' + kw - Tw'' - q \right] \delta w dx = 0$$
 (2 - 10)

Because δw is arbitrary for 0 < x < L, then the quantity within the brackets of equation 2-10 must always equal zero for the integral to always equal zero. This leads to the following differential equation describing the equilibrium of a straight beam on an elastic foundation,

$$EI(w'')'' - Tw'' + kw - q = 0$$

or,

$$EI\left(\frac{\partial^4 w}{\partial x^4}\right) - T\left(\frac{\partial^2 w}{\partial x^2}\right) + kw = q. \tag{2-11}$$

The oscillatory motion of a straight beam on an elastic foundation can now be obtained by allowing the distributed load q(x) to represent the D'Alembert force $-\rho \frac{\partial^2 w}{\partial t}$, which leads to the equation

$$EI\left(\frac{\partial^4 w}{\partial x^4}\right) - T\left(\frac{\partial^2 w}{\partial x^2}\right) + kw + \rho_m\left(\frac{\partial^2 w}{\partial t^2}\right) = 0. \tag{2-12}$$

where, t = time and $\rho_m =$ tread mass per unit length.

DERIVATION OF THE CRITICAL SPEED EQUATION

Critical speed is defined as the velocity at which a standing wave develops in the tread band. The critical speed equation is derived by considering an assumed mode as the wave solution to the governing differential equation (equation 2-12), taking the form

$$w = \sin a(x - vt) \tag{2-13}$$

where, a is a constant and v is the wave speed. Substituting equation 2-13 and its derivatives into equation 2-12 gives

$$EIa^4 + Ta^2 + k - \rho_m a^2 v^2 = 0.$$
 (2-14)

Centrifugal effects contribute to the tread tension (T). This implies that T is a function of velocity. It will be demonstrated in the discussion on structural properties that T will have the form

$$T = T_p(\text{pressure effect}) + \alpha v^2(\text{centrifugal effect})$$
 (2 - 15)

Since the centrifugal effect depends on tread band density, it may be combined with the acceleration term to give a modified density

$$\rho_m = \rho'(\text{effective density}) + \alpha(\text{centrifugal effect})$$
(2 - 16)

Substituting equations 2-15 and 2-16 into equation 2-14 yields

$$EIa^4 - (\rho'v^2 - T_p)a^2 + k = 0.$$
 (2-17)

The critical speed (V_{cr}) is the minimum speed that satisfies equation 2-17. Dr Clark^[2] solves equation 2-17 by expressing the equation in terms of two parameters M and N. M is associated with the wave speed v and N is a single parameter representing the tire properties. M and

N have unique values associated with the critical speed (V_{cr}) . The procedure for representing equation 2-17 in terms of M and N is as follows:

- 1. Let $N = \frac{EIa^4}{k}$ and $M = \frac{(\rho'v^2 T_p)^2}{EIk}$
- 2. In terms of M and N, equation 2-17 may be rewritten as

$$N - \sqrt{MN} + 1 = 0. ag{2 - 18}$$

3. Solving equation 2-18 for M gives

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$$M = \frac{1}{N}(N+1)^2. (2-19)$$

Because N is associated with the tire properties and M with the wave speed v, the minimum value of M satisfying equation 2-19 represents the unique value associated with the minimum speed (critical speed) satisfying the wave solution. The minimum value of M is obtained by solving for M in equation 2-19, differentiating with respect to N (the tire properties), setting the result equal to zero, solving for N, and substituting the value of N back into equation 2-19 to solve for the minimum value of M. It is found that the minimum value for M is 4.

To solve for the critical speed the value of 4 for M is substituted back into $M = \frac{(\rho' v^2 - T_p)^2}{ETk}$, and the equation solved for v, yielding

$$v = V_{cr}(\text{critical speed}) = \sqrt{\frac{T_p}{\rho'} + \sqrt{\frac{4kEI}{(\rho')^2}}}.$$
 (2 – 20)

TIRE STRUCTURAL PROPERTIES

Modeling the tread band of bias and radial tires as a beam on an elastic foundation is common practice for studying tire vibrations. The challenge in applying this method to aircraft tires is correctly describing those terms used in the critical speed equation. The following paragraphs give a description of each term.

Bending Stiffness (EI)

A widely used material in the carcass of aircraft tires is 840/2 Nylon. The fabric modulus of elasticity (E_f) is the effective modulus in the longitudinal direction of the nylon-rubber ply laminate, and is a function of the cord half angle γ . Figure 2 is a plot of E_f versus γ obtained from 840/2 Nylon-rubber tensile tests conducted by Dr Clark^[2].

The rubber tread modulus of elasticity (E_r) can vary from tire to tire and from manufacturer to manufacturer. The value of E_r is dependent on what compounds the manufacturer may use in the tread rubber. The tread will exhibit E_r values ranging from 500 psi to 2000 psi.

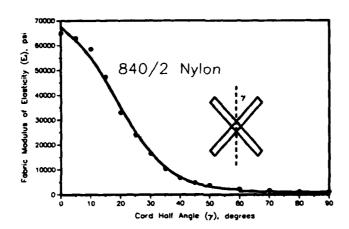


Figure 2. Fabric Modulus of Elasticity (E_f) versus Cord Half Angle (γ)

The bending stiffness (EI) is a function of E_f , E_r , the thickness of the rubber-tread region (t_r) , and the thickness of the cord-rubber fabric region (t_f) . Figure 3 shows a description of t_r and t_f . Bending stiffness (EI) can be expressed approximately as

$$EI = \frac{t_f^3 E_f}{12} + \frac{E_r}{4} [t_f^2 t_r + 2t_f t_r^2 + t_r^3] + \frac{E_r t_r^3}{12}$$
 (2 - 21)

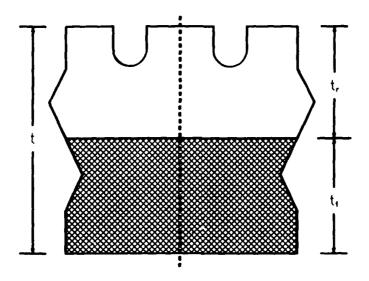


Figure 3. Tread cross-sectional parameters $t_{m{r}}$ and $t_{m{f}}$

Linear Spring Constant (k)

The linear spring constant k describes the elastic restraints provided by the combined effect of the tire internal inflation pressure and sidewall. k relates a force per unit area to vertical tire deflection and is defined as

$$k = \frac{p_r}{d_r} \tag{2-23}$$

where, p_r is the tire rated inflation pressure, and d_r is the rated tire deflection.

Belt Tension Due to Inflation Pressure (T_p)

The bias ply tire cross-sectional profile is idealized as the midline of the fabric structure as depicted by line O-A in Figure 4. Line O-A is divided into a tread region and sidewall region at the tire shoulder a-a. With the tire stationary, pressure forces are balanced by the carcass force F_c .

Referring to Figure 4 and taking moments about point O gives

$$F_c h = \frac{p_i h^2}{2} + \frac{p_i w_r^2}{2}. {(2-23)}$$

The tire section height (h) and w_r are related to an idealized cross-section radius of curvature (r) as

$$h = r\left(1 + \frac{\sqrt{2}}{2}\right)$$

$$w_r = r\frac{\sqrt{2}}{2}$$

from which

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$$w_r = \frac{\sqrt{2}h}{2 + \sqrt{2}}$$

Substituting for w_r into equation 2-23 and solving for F_c yields

$$F_c = 0.586 p_i h. ag{2-24}$$

The cord structure in a bias ply tire is illustrated in Figure 5. Let S be the collective cord load along the cord axis, l be the cord length, and γ be the cord half angle. In Figure 5, F_c and T_p are defined as

$$F_c = \frac{2S\sin\gamma}{l\cos\gamma} = \frac{2S\tan\gamma}{l} \tag{2-25}$$

$$T_p = \frac{2S\cos\gamma}{l\sin\gamma} = \frac{2S\cot\gamma}{l}$$
 (2 - 26).

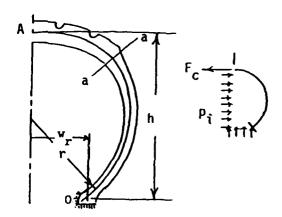


Figure 4. Idealized Shape Of the Bias Ply Tire Cross-Section

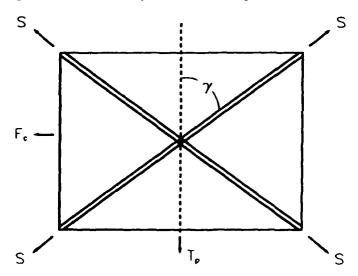


Figure 5. Cord Structure and Tensile Loads In a Bias Ply Tire

Combining equations 2-24 to 2-26 and rearranging gives the desired relation for the belt tension (T_p) as a function of inflation pressure, tire section height, and cord half angle.

$$T_p = 0.586 p_i h \cot^2 \gamma. (2-27)$$

Belt Tension Due to Centrifugal Effects (αv^2)

During rotation, the tire changes cross-sectional shape and grows to the shape depicted by line O-B in Figure 6. The horizontal carcass force F_c changes by an amount dF_c and the tread

centerline moves upward a distance dh. The new moment equilibrium equation about point O becomes

$$(F_c + dF_c)(h + dh) = \frac{p_i(h + d_h)^2}{2} + 0.0858p_ih^2 + Q(w_r - a)$$

where, Q is the centrifugal force equivalent to half the total centrifugal force acting on the cross-section, and a is the distance taken normal to the tire plane centerline from centerline to point of application of force Q. Retaining those terms associated with centrifugal effects and neglecting higher-order terms reduces the moment equilibrium equation due to centrifugal effects to

$$F_c dh + h dF_c = p_i h dh + Q(w_r - a). \qquad (2-28)$$

Recalling that $F_c=0.586p_ih$, substituting for F_c into equation 2-28, and solving for dF_c yields

$$dF_c = 0.414p_idh + \frac{Q(w_r - a)}{h}.$$
 (2 - 29)

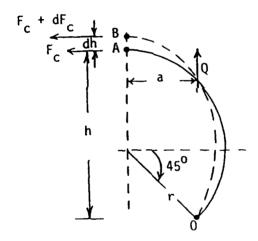


Figure 6. Change In Tire Cross-Sectional Shape During Rotation

Before equation 2-29 can be simplified to a usable form relations for Q, dh, and $(w_r - a)$ must be derived. In doing so, the overall cross-sectional shape is assumed to be circular as shown in Figure 7.

Defining ρ_1 as a mass per unit area of tire surface, then a differential mass element per unit width can be expressed as

$$dm = \rho_1 r d\theta$$
.

A differential centrifugal force dQ can be expressed as

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$$dQ = z\omega^2 dm$$
$$= z\omega^2 \rho_1 r d\theta$$

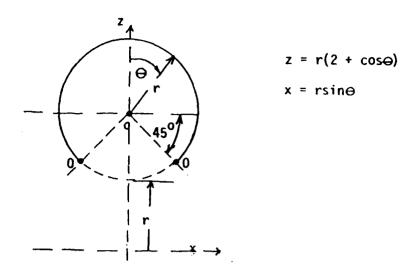


Figure 7. Circular Approximation to the Tire Cross-Sectional Shape

where ω is the tire rotational speed.

Integrating dQ from $0 \le \theta \le 3\pi/4$ gives a relation for Q as

$$Q = \omega^2 \int_0^{\frac{3\pi}{4}} r(2 + \cos\theta) \rho_1 r d\theta$$

$$= \rho_1 \omega^2 r^2 \frac{3\pi + \sqrt{2}}{2}$$

$$= 5.42 \rho_1 \omega^2 r^2. \tag{2 - 30}$$

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It is more convenient to express Q in terms of the total tire mass m_t . It is assumed that the mass per unit surface area (ρ_1) is constant over the tire surface. The value of m_t is obtained by integrating ρ_1 over the tire surface as follows:

$$\begin{split} m_t &= \rho_1 \; (\text{effective circumference}) \; \times \; (\text{crosssectional profile arc length}) \\ &= \rho_1 \; [2\pi (\text{radial centrold } \hat{y})] \; \times \; (\text{crosssectional profile arc length}) \\ &= \rho_1 \; \left[\frac{2\pi \int_0^{\frac{3\pi}{4}} r(2+\cos\theta) r d\theta}{\int_0^{\frac{3\pi}{4}} r d\theta} \right] 2 \int_0^{\frac{3\pi}{4}} r d\theta \\ &= 4\pi \rho_1 r^2 \int_0^{\frac{3\pi}{4}} (2+\cos\theta) d\theta \\ &= 68\rho_1 r^2. \end{split} \tag{2-31}$$

Solving equation 2-31 for ρ_1 and substituting the result into equation 2-30 leads to an expression for Q in terms of m_t which is expressed as

$$Q = 0.08 m_t \omega^2. (2 - 32)$$

Referring to Figure 7 and taking moments of Q about the origin yields

$$M_o = \int x dQ$$

$$= \omega^2 \int_0^{\frac{3\pi}{4}} r(2 + \cos \theta) \rho_1 r^2 \sin \theta d\theta$$

$$= 3.66 \rho_1 \omega^2 r^3.$$

The distance a is given by

$$a = \frac{M_o}{Q}$$

$$= \frac{3.66\rho_1 \omega^2 r^3}{5.42\rho_1 \omega^2 r^2}$$

$$= 0.675r$$

Recall that $w_r = \frac{r-\bar{2}}{2}$, giving

$$wr - a = \frac{r\sqrt{2}}{2} - .675r$$

$$= 0.032r.$$
(2 - 33)

From the NASA Technical Report R-64^[4] the radial growth (dh) due to centrifugal effects is expressed as

$$dh = \frac{0.01 m_l \omega^2}{p_i}. (2-34)$$

Substituting equations 2-32 to 2-34 into equation 2-29 yields

$$dF_c = 0.00414 m_t \omega^2 + \frac{0.00256 m_t r \omega^2}{h}.$$
 (2 - 35)

Noting that $h=r[1+\sqrt{2}/2]$ and $W_t=m_t g$, equation 2-35 becomes

$$dF_c = 1.461 \times 10^{-5} W_t \omega^2 \tag{2-36}$$

where, W_t is the tire weight in pounds, and g is the gravitational constant, 386.1 in/s^2 . From equations 2-25 and 2-26 the relation between dT and dF_c can be derived and expressed as

$$\frac{dT}{dF_c} = \cot^2 \gamma. \tag{2-37}$$

Combining equations 2-36 and 2-37 and replacing ω^2 by $(v/r_o)^2$ leads to the following expression for the belt tension due to centrifugal effects,

$$dT = 1.461 \times 10^{-5} W_t \left(\frac{v \cot \gamma}{r_o}\right)^2$$

$$= \alpha v^2$$
(2 - 38)

where,

$$r_o =$$
 tire rolling radius
$$\alpha = 1.461 \times 10^{-5} W_t \left(\frac{\cot \gamma}{r_o}\right)^2 \tag{2-39}$$

Effective Tread Density (ρ')

The effective tread density (ρ') takes into account the average tread mass density (ρ_m) and centrifugal effects (α) , and is expressed as

$$\rho' = \rho_m - \alpha.$$

The tread mass density (ρ_m) for a unit width of tread can be calculated from known specific weights of polymeric cord-rubber compounds of approximately 1.12 times that of water. The tread mass density as a function of tread thickness is

$$\rho_m = t \times 10^{-4}.$$

Subtracting the centrifugal effects (α) from the tread mass density leads to the effective density equation

$$\rho' = \left[t - 0.1461 W_t \left(\frac{\cot \gamma}{r_o} \right)^2 \right] \times 10^{-4}. \tag{2-40}$$

CRITICAL SPEED (V_{cr}) FOR RATED CONDITIONS

A sample critical speed calculation is presented at rated conditions for a 49x17/26PR Type VII Goodyear tire, KC-135 main landing gear tire, Serial Number 51400054. Rated conditions are:

- 1. Deflection of approximately 29%
- 2. Vertical load of 39600 pounds
- 3. Inflation pressure of 170 psl
- 4. Maximum speed of 225 mph

The following paragraphs present calculations for the individual terms comprising the critical speed equation and the critical speed prediction.

Values for the fabric modulus of elasticity (E_f) , rubber-tread modulus of elasticity (E_r) , thickness of rubber-tread region (t_f) , thickness of cord-rubber-fabric region (t_f) , and cord half angle (γ) must be acquired before the bending stiffness (EI) can be calculated. Goodyear engineers suggested that a value of 38° be used for γ and a value of 2175 psi be used for E_r .

Knowing γ and referring to Figure 2, a value of E_f was determined to be 8571 psi. Values for t_r and t_f were 0.7 and 0.535 inches. EI is calculated as

$$EI = \frac{t_f^3 E_f}{12} + \frac{E_r}{4} [t_f^2 t_r + 2t_f t_r^2 + t_r^3] + \frac{t_r^3 E_r}{12}$$

$$= \frac{(0.535)^3 (8571)}{12} + \frac{(2175)}{4} [(0.535)^2 (0.7) + 2(0.535)(0.7)^2 + (0.7)^3] + \frac{(2175)(0.7)^3}{12}$$

$$= 752 \text{ lbs} - \text{ln}.$$

The linear spring constant (k) is a function of the inflation pressure (p_i) and tire deflection (d). At rated conditions d is 29 percent of the section height (h), and is calculated to be 3.61 inches. The value of k is calculated as

$$k = \frac{p_r}{d_r}$$

$$= \frac{170}{3.61}$$

$$= 47.09 \frac{\text{lbs}}{\ln 3}.$$

The belt tension (T_p) due to inflation pressure is a function of inflation pressure (p_i) , the tire section height (h), and cord half angle (γ) . T_p is calculated as

$$T_p = 0.586 p_i h \cot^2 \gamma$$

= 0.586(170)(12.44) \cot^2(38°)
= 2030 lbs/ln.

The effective density term (ρ') is a function of the tread thickness (t), tire weight (W_t) , cord half angle (γ) , and tire rolling radius (r_o) . The tire weight at full tread depth was measured to be 187 pounds. r_o is defined as the tire undeflected outside radius minus one-third the tire deflection^[4], and was calculated to be 22.98 inches. ρ' is calculated as

$$\rho' = \left[t - 0.1461W_t \left(\frac{\cot \gamma}{r_o}\right)^2\right] \times 10^{-4}$$

$$= \left[1.235 - .1461(187) \left(\frac{\cot(38^\circ)}{22.98}\right)^2\right] \times 10^{-4}$$

$$= 1.150 \times 10^{-4} \frac{|bs - s^2|}{|n^3|}.$$

The critical speed $\left(V_{cr}\right)$ at rated conditions can now be calculated as

$$V_{cr} = \sqrt{\frac{T_p}{\rho'}} + \sqrt{\frac{4kEI}{(\rho')^2}}$$

$$= \sqrt{\frac{2030}{1.150 \times 10^{-4}}} + \sqrt{\frac{4(47.09)(752)}{(1.150 \times 10^{-4})^2}}$$

$$= 4574 \ln/s$$

$$= 260 \text{ mph.}$$

SECTION III

PARAMETRIC STUDY

This section describes how critical speed changes with tire inflation pressure, cord half angle, tread depth, and aspect ratio. All results presented are for the 49x17/26PR Type VII Goodyear tire, Serial Number 51400054.

CRITICAL SPEED VERSUS INFLATION PRESSURE

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Theory Indicates that critical speed is most sensitive to belt tension due to tire inflation pressure. In practice, a common method to delay the speed at which the standing wave develops is simply to increase tire operational inflation pressure. Tire operational inflation pressures of modern aircraft and future aerospace vehicle concepts approach flotation and runway structural limitations. Consequently, increasing the tire operational inflation pressure to delay critical speed may not be a viable solution. Figure 8 shows the sensitivity of critical speed to tire inflation pressure. Tire deflection is kept constant while pressure and load are varied.

CRITICAL SPEED VERSUS CORD HALF ANGLE

The belt tension due to inflation pressure is also highly dependent on cord half angle. Small changes in this half angle will yield significant changes in belt tension, and in turn, critical speed. Therefore, the value for cord half angle in critical speed predictions should be precise. The value for this angle used in the critical speed equation is the cord half angle taken at the tire crown. Figure 9 shows the sensitivity of critical speed to cord half angle. Tire deflection, load, and pressure are at rated values.

CRITICAL SPEED VERSUS TREAD DEPTH

Changes in tread depth incur changes in tire aspect ratio, section height, and weight. These changes affect the values for bending stiffness, belt tension due to inflation pressure, and effective tread density. Changes in tread depth can have a significant effect on critical speed. A reduction in tread depth will delay critical speed to higher values. Table 1 lists the effects of tread depth on the terms of the critical speed equation and critical speed prediction. All calculations are done at rated conditions.

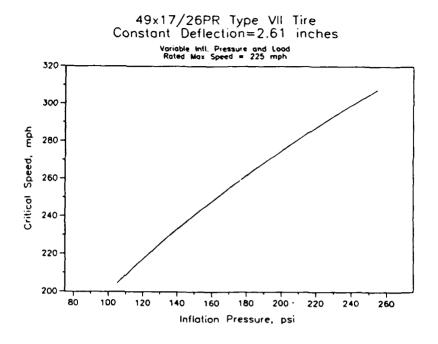
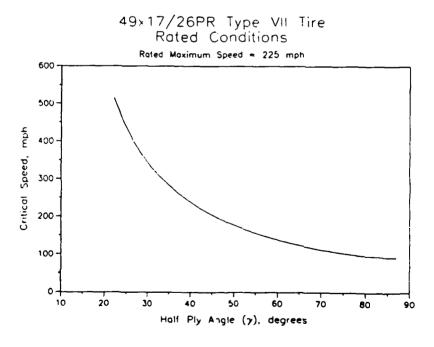


Figure 8. Critical Speed versus Inflation Pressure, 49x17/26PR Type VII Tire



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Figure 9. Critical Speed versus Cord Half Angle, 49x17/26PR Type VII Tire

TABLE 1. THE EFFECT OF TREAD DEPTH ON CRITICAL SPEED FOR A 49x17/26PR TYPE VII GOODYEAR TIRE, RATED CONDITIONS.

t	tr	h	EI	W_t	$\rho' \times 10^{-4}$	T_{p}	V _{cr}
1.235	0.700	12.44	752	187	1.150	2030	260
1.048	0.513	12.25	415	178	0.966	2000	276
0.844	0.309	12.05	229	166	0.766	1966	303
0.635	0.100	11.84	131	151	0.563	1932	346

where,

t =total tread thickness, inches

 $t_r = \text{rubber} - \text{tread depth}$, Inches

h = tire section height, inches

EI =bending stiffness, lbs - in

 $W_t = \text{tire weight, pounds}$

 $\rho' = \text{ effective tread density, lbs} - s^2/\text{in}^3$

 T_p = belt tension due to inflation pressure, lbs/in

 $V_{cr}=\,$ critical speed, mph.

CRITICAL SPEED VERSUS TIRE ASPECT RATIO

The tire aspect ratio (A_R) is a geometric parameter defined by the ratio of section height (h) to section width (u_{s}) . A_R can be expressed as

$$A_R = \frac{h}{w_s} = \frac{D_o - D}{2w_s} \tag{3-1}$$

where,

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 $D_o =$ tire outside diameter

D = wheel rim ledge diameter + (2 × flange height).

For this analysis, variations in tire aspect ratio are due to changes in section height while maintaining a constant section width. Tire percent deflection and vertical loads are kept constant. As a result, rated inflation pressure, vertical stiffness, and outside diameter must be adjusted. To estimate these adjustments a load/deflection relation for Type VII bias ply tires[4] was utilized. The relation is expressed as

$$F_z = 2.4w_s(p_i + 0.08p_r)\sqrt{(w_sD_o)}\left(\frac{d}{w_s} - C_z\left[1 - e^{(-0.6d/w_s)/C_z}\right]\right)$$
(3-2)

where,

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 F_z = vertical load, pounds

 $p_i = \text{inflation pressure, psi}$

 $p_r =$ rated inflation pressure, psi

 $w_s = \text{cross} - \text{sectional width, inches}$

 $D_o =$ outside tire diameter, inches

d = tire deflection, inches

 $C_z = \text{empirical constant}, \text{ approximately 0.03}.$

When considering only rated conditions (i.e., $p_i = p_r$) and using equation 3-1, then equation 3-2 can be expressed in terms of the tire aspect ratio as

$$F_z = 2.592 p_r w_s \sqrt{w_s (2w_s A_R + D)} \left(\frac{d}{w_s} - C_z \left[1 - e^{(-0.6d/w_s)/C_z} \right] \right)$$
(3 - 3)

The tire vertical stiffness (K_z) is obtained by taking the derivative of equation 3-3 with respect to tire deflection, yielding

$$K_z = 2.592 p_r \sqrt{w_s (2w_s A_R + D)} \left[1 - 0.6 e^{(-0.6d/w_s)/C_z} \right]$$
 (3 - 4)

The desired expression for K_z is obtained by solving equation 3-4 for p_r , substituting the result into equation 3-3, and rearranging. This leads to an expression for K_z given by

$$K_z = \frac{F_z}{w_s} \frac{1 - 0.6e^{(-0.6d/w_s)/C_z}}{\frac{d}{w_s} - C_z \left[1 - e^{(-0.6d/w_s)/C_z}\right]}$$
(3 - 5)

The 49x17/26PR Type VII Goodyear tire is used as a baseline defining constant values for rated load, percent deflection, and section width. A section width (w_s) of 16.92 inches was measured for the subject tire. By fitting equation 3-2 to experimental load/deflection data a value of 0.0337 for C_z was obtained. D for the 49x17/26PR tire is 23.5 inches. For rated load $(F_z=39600 \text{ lbs})$ and percent deflection (29%), the data in Table 2 was generated along with calculated critical speeds using equations 2-20, 3-1, 3-3, and 3-5.

TABLE 2. THE EFFECT OF TIRE ASPECT RATIO ON CRITICAL SPEED FOR A 49x17/26PR TYPE VII GOODYEAR TIRE AS A BASELINE, RATED CONDITIONS.

A_r	h (Inches)	D_o (inches)	d (Inches)	K_z (lbs/in)	p _r (psi)	$rac{V_{cr}}{ ext{(mph)}}$
1.0	16.92	57.34	4.91	9087	113	236
0.9	15.23	53.96	4.42	10213	131	243
8.0	13.54	50.57	3.93	11642	155	252
0.7	11.84	47.19	3.43	13653	189	263
0.6	10.15	43.80	2.94	16080	234	275
0.5	8.46	40.42	2.45	19654	304	292

The data of Table 2 Indicate that thre aspect ratio has a significant effect on critical speed. By maintaining constant section width for variations in thre aspect ratio, the values of section height and inflation pressure must be adjusted for a given rated load and percent deflection. Both section height and inflation pressure contribute to the belt tension due to inflation pressure; belt tension having the greatest influence on critical speed. Again, thre operational inflation pressure limits may dictate a lowest practical thre aspect ratio.

SECTION IV

VALIDATION

This section describes the tests conducted to provide full-scale tire laboratory data for validation of the analytical techniques used in predicting critical speed. The KC-135 49X17, 26 ply rating, tire was used as a baseline to establish dynamometer test methodology for high speed operational assessment (inertia effects/critical speed) of current tire design limitations. This tire size was selected as the baseline because of its availability, high-speed (224 MPH), and high-load (39,600 lbs) capability.

TEST MATRIX

A detailed test matrix, Table A-1, Appendix , was prepared to establish the critical speed $(V_{\rm cr})$ limitations of the baseline 49X17 tire at various test conditions.

Test series 1P&L through 6P&L, and 14P&L through 16 P&L were to be conducted at constant load (39600 lbs. flat plate and rated) to determine the effect of pressure, deflection, and mold skild depth on critical speed. The mold skild depth or the groove depth is defined as the thickness of tread between the tire's outer tread surface and the bottom of the tread groove.

Test series 4P&L, 5P&L, 7P&L through 11P&L, and 17P&L through 19P&L were to be conducted at rated deflection (170 PSI inflation pressure and 39600 LBS flat plate and rated load) to determine the effect of pressure load and mold skid depth on critical speed.

Test series 4P&L, 5P&L, 12P&L, and 17P&L through 31P&L were to be conducted at constant pressure to determine the effect of load and deflection on critical speed.

TEST METHOD

All critical speed tests were conducted in the AFWAL Landing Gear Development Facility using the 120-inch programmable dynamometer. The 49X17/26PR tires were taken from the same manufacturer (Goodyear), production lot (serial numbers 50280284 through 53570337), and qualification (QTR 461B-2049-TL). In each of the 62 test series listed in the Test Matrix, a different 49X17/26PR test tire was to be used.

Tire Preparation and Break-in

All test tires were subjected to a 12 hour stretch and a 24-hour air-retention check in accordance with MIL-T-5041 [5]. The rated inflation pressure of 170 PSI was used. Tires were buffed to the specified mold skid depth (0.10 or 0.30 inches) as applicable per the Test Matrix. Tires were buffed uniformly across the full width of the tread by Air Treads, Inc. After buffing, new weight and unbalance data were obtained. Each test tire was conditioned by conducting a taxi roll on the dynamometer for 2 miles at 39600 LBS rated load and at 30 MPH constant speed.

Test Procedure

Correction for flywheel curvature was accomplished by pressure adjustment for test series 1P through 31P. At the specified flat plate inflation pressure, the correction for flywheel curvature was made by increasing the pressure to obtain the desired deflection. Flat plate and flywheel tire deflection data was obtained.

Correction for flywheel curvature was accomplished by load adjustment for test series 1L through 31L. At the specified flat plate inflation pressure, the correction for flywheel curvature was made by reducing the load on the flywheel to obtain the desired deflection. Flat plate and flywheel tire deflection data was obtained.

Correction for flywheel curvature by load reduction is the preferred adjustment in lieu of pressure increase. Pressure increase results in a much higher critical speed, in some cases far exceeding the rated speed of the tire. Thus, premature failures due to tread rotational inertia and adhesion limitations are likely to occur before critical speed is reached as predicted.

Initially, the first test velocity listed in each test series was approximately 20 percent lower than the calculated V_{cr} value. As the confidence level increased with the use of the V_{cr} prediction techniques, the first test velocity was set approximately 10 percent lower than the calculated value. Subsequent test cycles were performed by increasing the test velocity in increments of either 5 or 10 MPH until the critical speed was reached. Once V_{cr} was reached, testing was continued until tire failure occurred. Each test cycle was recorded on videotape.

To prevent tire slippage during spin-up on the dynamometer, the tire was lightly loaded against the stationary flywheel. Then the flywheel was brought up to the test velocity using maximum acceleration and the tire was further loaded to the specified test load.

For each test cycle, at the specified constant normal load, the velocity was held at steady-state for a limited duration. At the end of the test cycle, the tire was unloaded from the flywheel and the contained air temperature was allowed to cool to $75 \pm 10^{\circ}$ F before proceeding to the next higher velocity increment. The test duration was initially set at 3 seconds per cycle, but

was considered too short a time duration to visually observe tire deformation at $V_{\rm cr}$. The test duration was then doubled, but the 6-second duration resulted in the entire tread stripping resulting in damage to the test equipment. Finally, a 4-second test duration was adopted and used throughout the remaining tests.

A painted grid on the tire's sidewall was used on the first few tires tested. This approach was terminated since there was no visual evidence of deformation in the sidewall during $V_{\rm cr}$.

TEST RESULTS

A series of dynamometer tests were conducted to validate the predicted V_{cr} trends including the effects of inflation pressure, mold skid depth, normal load, and deflection. A limited number of V_{cr} test series, as specified in the Test Matrix, have been conducted on the 49X17/26PR baseline tire.

Results of the V_{cr} tests to date are summarized in Table 3. As shown in this table, the predicted V_{cr} values are very near the experimental values, within +13.3 percent and -1.5 percent with an average of 2.9 percent.

In evaluating the baseline tire's test results, the following trends were observed based on the limited tests performed:

Effect Of Inflation Pressure

Trend data in terms of V_{cr} versus inflation pressure is shown in Figure 10. Results show that the predicted (V_{cr-p}) and experimental (V_{cr-e}) critical speeds increased significantly as the inflation pressure is increased. As illustrated in this figure, this trend holds true for the three different mold skid depth levels investigated. Each data point in the figure represents a separate test tire in a given test series.

As observed from Figure 10, the critical speed values predicted from the analytical model are in good agreement with the experimental values. Even over the wide pressure (102 to 197 PSI) range and mold skid depth (0.125 to 0.53 inches) range, there is generally good agreement between V_{cr-e} and V_{cr-p} results.

TABLE 3. CRITICAL SPEED COMPARISONS: PREDICTED (V_{cr-p}) VERSUS EXPERIMENTAL (V_{cr-e}) .

	TEST	PRESS.	%	LOAD	V_{cr-p}	V_{cr-e}	%
TIRE	SERIES	(psl)	DEFL.	(lbs)	(mph)	(mph)	DIFF.
		a) Full Tre	ad Depth (0.47 to 0.53	inches)	·	·
2-N	1P	125	48.3	39600	217	210	3.3
3-N	1P	125	48.0	39600	218	215	1.4
4-N	1L	102	42.5	31500	197	200	-1.5
4-N	1L	102	42.5	31500	197	200	-1.5
5-N	4 P	197	28.9	39600	272	240	13.3
6-N	4 P	197	28.5	39600	275	245	12.2
12-N	4L	170	29.7	34500	254	*	_
20-N	7P	125	29.6	25700	222	220	0.9
19-N	7L	102	29.7	21900	202	205	1.5
21-N	12P	197	20.0	24700	278	*	_
29-N	17L	136	28.9	28000	234	*	_
31-N	20L	136	20.0	18000	236	240	-1.5
32-N	14L	136	34.2	34000	231	*	_
33-N	26L	102	20.0	14500	204	215	5.1
34-N	4L	170	28.5	34500	255	245	4.1
38-N	12L	170	20.0	22300	261	260	0.4
40-N	14L	136	33.8	33600	231	*	-
41-N	17L	136	28.7	27500	230	*	-

Notes: * Tread failure occurred prior to an onset of the standing wave.

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^{**} No standing wave was observed at this low (10%) tire deflection.

TABLE 3. (CONCLUDED)

	TEST	PRESS.	%	LOAD	V_{cr-p}	V _{cr-e}	%				
TIRE	SERIES	(psl)	DEFL.	(lbs)	(mph)	(mph)	DIFF.				
	b) Intermediate Tread Depth (0.31 to 0.34 inches)										
7-N	2P	125	48.5	39600	232	230	2.7				
8-N	2P	125	48.3	39600	231	225	2.7				
9-N	2L	102	41.8	33300	211	210	0.5				
10-N	8P	119	29.0	25000	230	225	2.2				
11-N	8L	102	29.7	21900	212	210	1.0				
13-N	15P	158	33.8	39600	262	*	-				
14-N	15L	136	34.4	33900	246	235	4.7				
17-N	18L	136	28.3	27800	248	240	3.3				
16-N	21L	136	20.0	18500	248	250	-0.8				
18-N	24L	136	10.0	7700	255	**	-				
42-N	27L	102	20.0	13000	220	225	-2.3				
	<u> </u>	c) Shallow T	read Depth	(0.09 to 0.	14 inches)						
22-N	3L	102	42.4	34000	222	225	-1.2				
23-N	9L	102	29.3	22100	234	225	4.0				
24-N	19L	136	28.9	27830	268	265	1.1				
25-N	16L	136	33.9	34000	270	270	0				
26-N	22L	136	20.0	18000	274	270	1.5				
28-N	28L	102	20.0	14000	237	245	3.3				
27-N	3P	125	42.2	39600	261	*	-				

Notes: * Tread fallure occurred prior to an onset of the standing wave.

^{**} No standing wave was observed at this low (10%) tire deflection.

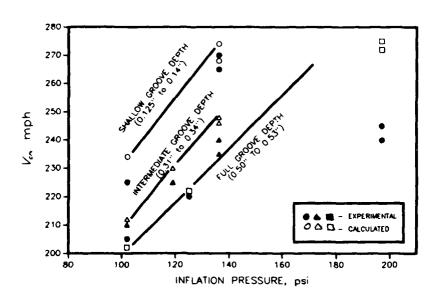


Figure 10. V_{cr} versus Inflation Pressure for the Various Mold Skid Depths. Normal Deflection Range (28% to 34%)

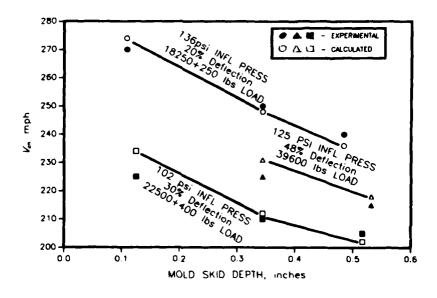


Figure 11. V_{cr} versus Mold Skid Depth for Various Inflation Pressure and Load Combinations

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Effect Of Mold Skid Depth

Trend data in terms of V_{cr} versus mold skild depth is shown in Figure 11 for various inflation pressure and load combinations. Both experimental and predicted results showed that as the tire's mold skild depth is reduced, the critical speed increases significantly. Again, there is relatively good agreement between the predicted and experimental results.

For the shallow mold skid depth of 0.11 to 0.14 inches a standing wave occurs in the shoulder region approximately 5 to 25 MPH sooner than the onset of the standing wave in the tread region. The higher the tire's operating deflection, the greater the speed differential of a standing wave occurring between the shoulder and the tread. For example, at 42 percent tire deflection (test series 3L), standing waves occurred at 200 MPH in the shoulder region and at 225 MPH in the tread region, a differential of 25 MPH. However, at the lower tire deflection of 20 percent (test series 22L) the speed differential was only 5 MPH.

Effect Of Normal Load

Trend data in terms of V_{cr} versus normal load is shown in Figures 12 and 13. Both predicted and experimental values showed that changes in the tire's normal load had little influence on the tire's critical speed. This trend holds true for the baseline tire at other inflation pressure conditions as well as for the different mold skild depths investigated.

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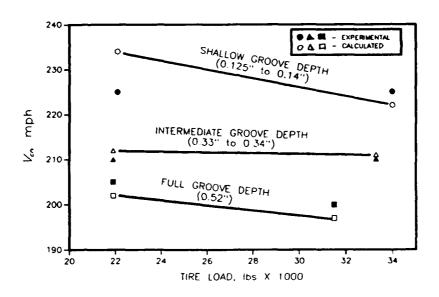
Effect Of Tire Deflection

Trend data in terms of V_{cr} versus tire deflection is shown in Figures 14 and 15. Both predicted and experimental results showed that changes in percent deflection had an insignificant impact on the baseline tire's critical speed. This trend holds true for the baseline tire at the three different mold skid depth levels as well as for the various inflation pressures investigated to date. A typical comparison of experimental and predicted V_{cr} (using an expanded scale) is illustrated in Figure 15 for the baseline tire at 136 PSI inflation pressure, intermediate groove depths, and over a 20 to 34 percent deflection range. There is good agreement between the predicted and experimental results, with differences ranging between +0.8 and -4.7 percent for this one set of conditions. This comparison is typical for all conditions.

Failure Mode/Location.

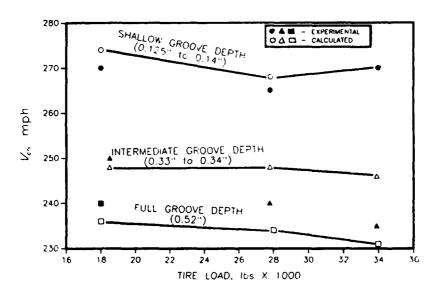
Failure mode and failure location are dependent on mold skid depth, test duration, tire deflection, and predicted critical speed. The predominant failure mode during $V_{\rm cr}$ tests was

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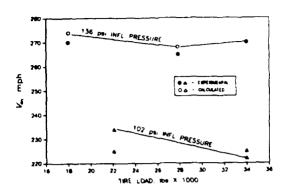


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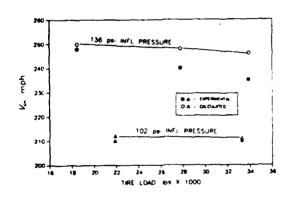
a) 102 psi Inflation Pressure (0.6 \times Rated)



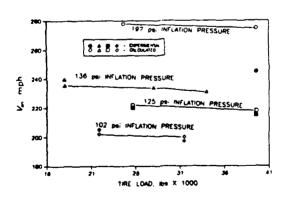
b) 136 psi Inflation Pressure (0.8 \times Rated) Figure 12. V_{cr} versus Tire Load at Two Inflation Pressures



a) Shallow Groove Depth (0.11 to 0.14 inches)



b) Intermediate Groove Depth (0.31 to 0.34 inches)



c) Full Groove Depth (0.47 to 0.53 inches)

Figure 13. V_{cr} versus Tire Load for Various Groove Depths

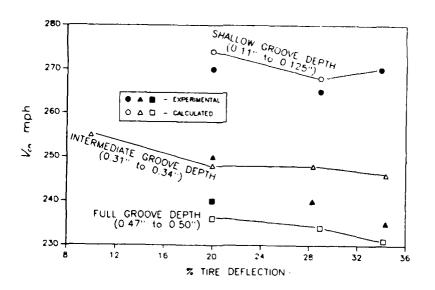


Figure 14. V_{cr} versus Percent Deflection for 49×17/26PR Tire at 136 psi Inflation Pressure for the Various Mold Skid Depths

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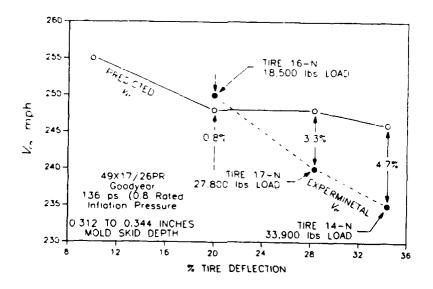


Figure 15. V_{cr} versus Percent Deflection for 136 psi Inflation Pressure and 0.328 (\pm 0.12) inches Mold Skid Depth

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tread separation. Initially, groove cracking was observed, then progressed to tread undercutting and subsequent tread chunking.

All failures that occurred on tires at full mold skid depth (0.52 inches) were due to tread chunking in the center rib. In 4 of the test series (4L, 12P, 14L and 17L), tires at the full mold skid depth failed prematurely before reaching the predicted $V_{\rm cr}$. A typical failure at full mold skid depth is shown in Figure 16.

Groove cracking appeared at the outer grooves when operating at higher deflections (40 percent range) for an intermediate mold skid depth of 0.3 inches, test series 2P and 2L (Figure 17). The failure location would shift toward the center rib and tread chunking would occur when operating in the normal deflection range (20 to 33 percent), test series 8L, 15P, 15L (Figure 18), 18L and 21L. No visible failure occurred when operating at 10 percent deflection (test series 24L). Also, there was no indication of V_{cr} when operating at this low deflection.

For the shallow mold skid depth of 0.1 Inches, tread chunking would occur at the shoulder ribs when the predicted critical speed was low, (222 MPH test series 3L to 234 MPH in test series 9L). However, when the predicted V_{cr} was high, (268 MPH in test series 19L, 270 MPH in test series 16L and 274 MPH in test series 22L), the tread chunking failure location shifted to the center rib.

The most severe tread chunking occurred during the longest test duration used (6 seconds). In test series 1P and 4P, the entire tread stripped during the 6-second duration of the first cycle on each tire (tire code 3-N and 6-N, respectively). As previously discussed under the Test Method subsection, a 4-second test duration was adopted and used throughout the remaining tests.

Experimental V_{cr} Criteria

The most successful method used in determining the occurrence of a standing wave in the tread band is to visually observe its inception. Tread elements transition from the tire footprint to a free rolling radius through a smooth radius of curvature for speeds well below $V_{\rm cr}$. The transition radius of curvature decreases significantly as $V_{\rm cr}$ is approached. This is exhibited by the tread elements growing into the flywheel and is consider the inception of the standing wave. Radial displacement of the tread continues to increase with speed and propagate along the tire circumference in the sinusoidal fashion. The speed associated with the standing wave inception is $V_{\rm cr}$. This method proved to be acceptable for tire deflections above 20 percent. Because of the low displacement amplitudes at tire deflections less than 20 percent, it was difficult to the inception of the standing wave. Large increases in drag force and rolling resistance, were not observed at critical speed in most test cases as originally expected. One good example where

drag force suddenly increased at critical speed is in test series 15L (test tire code 14-N). The inception of a standing wave in this test series was first noticed at 235 MPH. At 240 MPH, the minimum and maximum drag force values increased by 385 and 194 percent respectively, and the maximum rolling resistance had increased by 180 percent over those values of the previous test run.

An increase in noise level was usually accompanied with a visual detection of the standing wave, indicating the initial stages of failure, i.e., tread chunking and tread stripping. However, an increase in noise level is not solely a positive indicator of critical speed. Increases in noise level can also occur when tires fail prematurely (prior to reaching V_{cr}) or after exceeding the V_{cr} and then failing at higher speeds.

Repeatability of results between two tires was demonstrated in test series 1P and 4P. In test series 1P, tires 2-N and 3-N had predicted critical speeds of 217 and 218 MPH, respectively, and experimental critical speeds of 210 and 215 MPH, respectively. In test series 4P, tires 5-N and 6-N had predicted critical speeds of 272 and 275 MPH, respectively, and experimental critical speeds of 240 and 245 MPH, respectively.

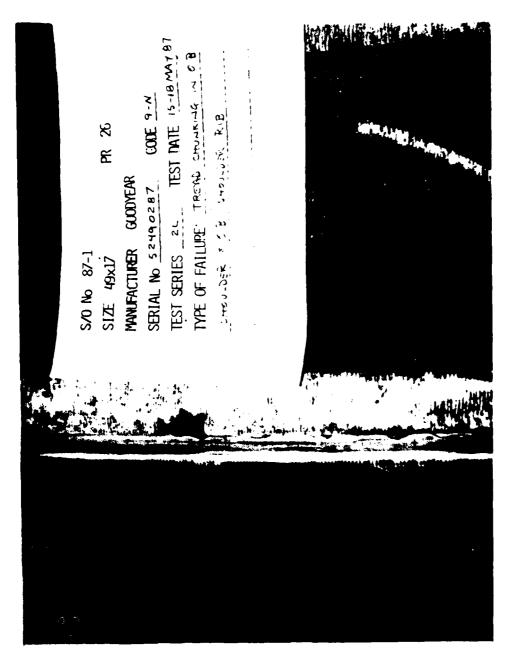
Repeatability of results with one tire was also demonstrated using tire 2-N in test series 1P. The onset of a standing wave was observed in two separate test runs on this tire at a critical speed of 210 MPH, prior to tread failure.

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S/0 No 87-1 SIZE 49x17 PR 26 MANUFACTUR**E**R GOODYEAR SERIAL No 50280300 CODE 12-N TEST SERIES 4L TEST DATE 6 MAY 87 TYPE OF FAILURE TREAD STUNKING IN CENTER BIB , E 22 IN.

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Figure 16. Typical Tread Failure at Center Rib. Full Mold Skid Depth. Tire Code 12-N, Test Series 4L.



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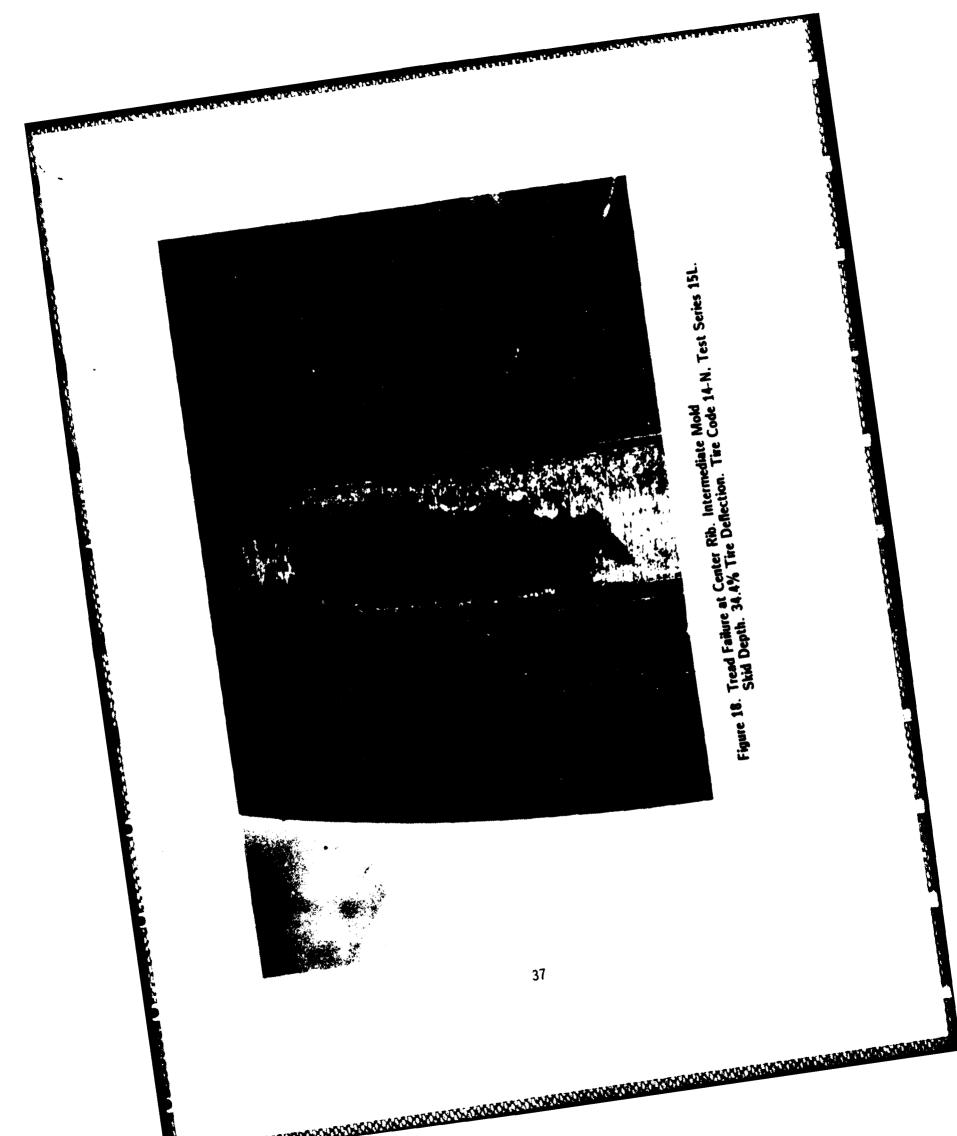
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b) Tread Chunking and Groove Cracking in Outboard Rib.

a) Close-up of Groove Cracks.

Figure 17. Typical Tread Failure at Outboard Rib. Intermediate Mold Skid Depth. 41.8% Tire Deflection. Tire Code 9-N. Test Series 2L.



SECTION V

CONCLUSIONS AND RECOMMENDATIONS

- 1. Both the analytical and experimental results showed that the major parameters affecting critical speed are inflation pressure and mold skild depth. Changes in normal load and in percent deflection had little influence on the tire's critical speed.
- 2. The critical speed values predicted from the analytical model are in good agreement with the experimental values observed during the initial tests on the baseline tire.
- 3. Alternate methods should be explored for the detection of the standing wave. The visual cue used during this study is subjective and does not represent a definitive indication of the onset of a standing wave.
- 4. Other causes such as purely centrifugal effects may account for tread retention failure prior to the onset of a standing wave. These types of failure were observed to take place at inflation pressures equal to or greater than rated inflation pressure and with full mold skid depth.
- 5. Critical speed is sensitive to the crown cord half angle. For this reason, an accurate value for the crown cord half angle should be used for quantitative prediction purposes.

6. Baseline tires from another vendor (B.F.Goodrich), other tire sizes (25.5x8.0-14/18PR/250 MPH and 34.5x9.75-18/26PR/259 MPH), and the radial tire should be included in the critical speed study.

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- 2. Technology Needs for High Velocity Vehicle Aircraft Tires, S.K. Clark, Precision Measurement Company, February 1987.
- 3. Tire Vibration, G.R. Potts, C.A. Bell, L.T. Charek and T.K. Roy, Tire Science and Technology, TSTCA, Vol. 5, No. 4, Nov. 1977, pp. 202-225.
- 4. NASA-TR-R-64, Mechanical Properties of Pneumatic Tires with Special Reference to Modern Aircraft Tires, R.F. Smiley and W.B. Horne, Langley Research Center, 1960.
- 5. MIL-T-5041G, Military Specification—Tires, Pneumatic, Aircraft, 12 September 1975.

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APPENDIX

TEST MATRIX — CRITICAL SPEED $49 \times 17/26$ PR, TYPE VII, TIRE.

TABLE A-1

<u></u>					
TEST CYCLE NR.	TEST VEL. (mph)	GROOVE DEPTH (Inches)	INFLATION PRESSURE (psl)	NORMAL LOAD (lbs)	TEST DEFL.
1P160 1P170 1P180 1P* 1PV _{cr}	160 170 180 * V _{cr}	0.52 (FULL)	102 psi (F.P.), ADJUST PRESS FOR F.W. CURVA-	39600	= F.P. DEFL @ 102 psi & 39600 lbs LOAD
2P180 2P* 2PV _{cr}	180 * V _{cr}	0.30	TURE		
3P200 3P* 3PV _{cr}	200 * V _{cr}	0.10			
1L160 1L170 1L180 1L* 1LV _{cr}	160 170 180 * V _{cr}	0.52 (FULL)	102 pst	39600 lbs (F.P.), ADJUST LOAD FOR F.W. CURVA-	= F.P. DEFL © 102 psi & 39600 lbs LOAD
2L180 2L* 2LV _{cr}	180 * V _{cr}	0.30		TURE	
3L200 3L* 3LV _{cr}	200 * V _{cr}	0.10			

NOTES:

- * Continue to increase the test speed in increments of 5 or 10 mph in subsequent test cycles until the critical speed $(V_{c\tau})$ is reached.
- (1) F.P. flat plate, F.W. flywheel
- (2) The second character in the test cycle number identifies the method taken to compensate for flywheel curvature, either by pressure ("P") increase or by load ("L") reduction.
- (3) All approximations (≈) were obtained from load-deflection curves, Goodyear report QTR 461B-2049-TL, 49x17/26PR tire.
- (4) Groove depth.- the mold skid depth or the groove depth after buffing.

TABLE A-1. (CONTINUED)

TEST CYCLE NR.	TEST VEL. (mph)	GROOVE DEPTH (Inches)	INFLATION PRESSURE (psl)	NORMAL LOAD (lbs)	TEST DEFL.
4P210 4P220 4P230 4P* 4PV _{cr}	210 220 230 * V _{cr}	0.52 (FULL)	170 psi (F.P.), ADJUST PRESS FOR F.W. CURVA- TURE	39600 lbs	= F.P. DEFL © 170 psi 39600 lbs LOAD
5P230 5P* 5PV _{cr}	230 * V _{cr}	0.30			
6P230 6P240 6P250 6P* 6PV _{cr}	230 240 250 * V _{cr}	0.52 (FULL)	204 psi (F.P.) ADJUST PRESS FOR F.W. CURVA- TURE		= F.P. DEFL @ 204 psi & 39600 lbs LOAD
4L210 4L220 4L230 4L* 4LV _{cr}	210 220 230 * V _{cr}	0.52 (FULL)	170 psi	39600 lbs (F.P.), ADJUST LOAD FOR F.W. CURVA- TURE	= F.P. DEFL © 170 PSI & 39600 lbs LOAD
5L230 5L* 5LV _{cr}	230 * V _{cr}	0.30			
6L230 6L240 6L250 6L* 6LV _{cr}	230 240 250 * V _{cr}	0.52 (FULL)	204 psi	39600 lbs (F.P.), ADJUST LOAD FOR F.W. CURVA- TURE	= F.P. DEFL @ 204 psi & 39600 lbs LOAD

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(1) F.P. - flat plate, F.W. - flywheel

^{*} Continue to increase the test speed in increments of 5 or 10 mph in subsequent test cycles until the critical speed (V_{cr}) is reached.

⁽²⁾ The second character in the test cycle number identifies the method taken to compensate for flywheel curvature, either by pressure ("P") increase or by load ("L") reduction.

⁽³⁾ All approximations (≈) were obtained from load-deflection curves, Goodyear report QTR 461B-2049-TL, 49x17/26PR tire.

TABLE A-1. (CONTINUED)

TEST CYCLE NR.	TEST VEL. (mph)	GROOVE DEPTH (Inches)	INFLATION PRESSURE (psl)	NORMAL LOAD (lbs)	TEST DEFL.	
7P170 7P180 7P190 7P* 7PV _{cr}	170 180 190 * V _{cr}	0.52 (FULL)	102 psi (F.P.), ADJUST PRESS FOR F.W. CURVA- TURE	ADJUST PRESS FOR F.W. CURVA-	≈ 27500 lbs © 102 psi F.P. & SPECIFIED DEFL	= F.P. DEFL © 170 psl & 39600 lbs LOAD
8P180 8P* 8PV _{cr}	180 * V _{cr}	0.30			TORE	
9P200 9P* 9PV _{cr}	200 * V _{cr}	0.10				
7L170 7L180 7L190 7L* 7LV _{cr}	170 180 190 * V _{cr}	0.52 (FULL)	102 psi	© ≈ 27500 lbs F.P. LOAD, ADJUST LOAD, LOAD FOR F.W. CURVA-		
8L180 8L190 8L* 8LV _{cr}	180 190 * V _{cr}	0.30		TURE		
9L200 9L* 9LV _{cr}	200 * V _{cr}	0.10				

NOTES:

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* Continue to increase the test speed in increments of 5 or 10 mph in subsequent test cycles until the critical speed (V_{cr}) is

reached.
(1) F.P. - flat plate, F.W. - flywheel

(2) The second character in the test cycle number identifies the method taken to compensate for flywheel curvature, either by pressure ("P") increase or by load ("L") reduction.

(3) All approximations (≈) were obtained from load-deflection curves. Goodyear report QTR 461B-2049-TL, 49x17/26PR

TABLE A-1. (CONTINUED)

TEST CYCLE NR.	TEST VEL. (mph)	GROOVE DEPTH (Inches)	INFLATION PRESSURE (psl)	NORMAL LOAD (lbs)	TEST DEFL.
10P230 10P240 10P* 10PV _{cr}	230 240 * V _{cr}	0.52 (FULL)	204 psi (F.P.) ADJUST PRESS CURVA- TURE	≈ 46000 lbs © 204 psi F.P. & SPECIFIED DEFL	= F.P. DEFL @ 170 psi & 39600 lbs LOAD
11P250 11P* 11PV _{cr}	250 * V _{cr}	0.30			
10L230 10L240 10L* 10LV _{cr}	230 240 * V _{cr}	0.52 (FULL)	204 psi	© ≈46000 lbs F.P. LOAD, ADJUST LOAD FOR F.W.	
11L250 11L260 11L* 11LV _{cr}	250 260 * <i>V_{cr}</i>	0.30		CURVA- TURE	

(1) F.P. - flat plate, F.W. - flywheel

Continue to increase the test speed in increments of 5 or 10 mph in subsequent test cycles until the critical speed (V_{cr}) is reached.

⁽²⁾ The second character in the test cycle number identifies the method taken to compensate for flywheel curvature, either

by pressure ("P") increase or by load ("L") reduction.

(3) All approximations (≈) were obtained from load-deflection curves, Goodyear report QTR 461B-2049-TL, 49x17/26PR

TABLE A-1. (CONTINUED)

TEST CYCLE NR.	TEST VEL. (mph)	GROOVE DEPTH (Inches)	INFLATION PRESSURE (ps1)	NORMAL LOAD (lbs)	TEST DEFL.
12P220 12P230 12P240 12P* 12PV _{cr}	220 230 240 * V _{cr}	0.52 (FULL)	170 psi (F.P.) ADJUST PRESS FOR F.W. CURVA- TURE	≈ 24500 (lbs) © 170 psl psl F.P. & 20% DEFL	20% DEFL, (≈2.52 INCHES)
13P220 13P230 13P* 13PV _{cr}	220 230 * V _{cr}			≈10500 lbs © 170 psi psi F.P. & 10% DEFL	10% DEFL, (≈1.26 INCHES)
12L220 12L230 12L240 12L* 12V _{cr}	220 230 240 * V _{cr}		170 psl	② ≈24500 lbs F.P. LOAD, ADJUST LOAD FOR F.W. CURVATURE	20% DEFL. (≈2.52 INCHES)
13L220 13L230 13L240 13L* 13V _{cr}	220 230 240 * V _{cr}			© ≈10500 lbs F.P. LOAD, ADJUST LOAD FOR F.W. CURVATURE	10% DEFL, (≈1.26 INCHES)

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- * Continue to increase the test speed in increments of 5 or 10 mph in subsequent test cycles until the critical speed (V_{cr}) is reached.
- (1) F.P. flat plate, F.W. flywheel
- (2) The second character in the test cycle number identifies the method taken to compensate for flywheel curvature, either
- by pressure ("P") increase or by load ("L") reduction.

 (3) All approximations (≈) were obtained from load-deflection curves, Goodyear report QTR 461B-2049-TL, 49x17/26PR
- (4) Groove depth .- the mold skid depth or the groove depth after buffing.

TABLE A-1. (CONTINUED)

TEST CYCLE NR.	TEST VEL. (mph)	GROOVE DEPTH (Inches)	INFLATION PRESSURE (psl)	NORMAL LOAD (lbs)	TEST DEFL.
14P190 14P200 14P* 14PV _{cr}	190 200 * V _{cr}	0.52 (FULL)	136 psi (F.P.), ADJUST PRESS FOR F.W. CURVA-	39600	= F.P. DEFL © 136 psi & 39600 lbs LOAD
15P210 15P* 15PV _{cr}	210 * V _{cr}	0.30	TURE		
16P220 16P* 16PV _{cr}	220 * V _{cr}	0.10			
14L180 14L* 14LV _{cr}	180 * V _{cr}	0.52 (FULL)	136 psi	39600 lbs (F.P.), ADJUST LOAD	
15L190 15L* 15LV _{cr}	190 * V _{cr}	0.30		FOR F.W. CURVA- TURE	
16L200 16L* 16LV _{cr}	200 * V _{cr}	0.10			

- NOTES:

 * Continue to increase the test speed in increments of 5 or 10 mph in subsequent test cycles until the critical speed (V_{cr}) is reached.
- (1) F.P. flat plate, F.W. flywheel
- (2) The second character in the test cycle number identifies the method taken to compensate for flywheel curvature, either by pressure ("P") increase or by load ("L") reduction.

 (3) All approximations (≈) were obtained from load-deflection curves, Goodyear report QTR 461B-2049-TL, 49x17/26PR
- tire.
- (4) Groove depth. the mold skid depth or the groove depth after buffing.

TABLE A-1. (CONTINUED)

TEST CYCLE NR	TEST VEL (mph)	GROOVE DEPTH (Inches)	INFLATION PRESSURE (psi)	NORMAL LOAD (lbs)	TEST DEFL.
17P100 17P* 17PV ₂ ,	190 * V _{cr}	0.52 (FULL)	136 psl (F.P.), ADJUST PRESS FOR F.W.	≈ 33000 lbs @ 136 psl F.P. & SPECIFIED	= F.P. DEFL @ 170 psi & 39600 lbs LOAD
18P210 18P* 18PV _{cr}	210 * V _{cr}	0.30	CURVA- TURE	DEFL.	
19P230 19P* 19PV _{cr}	230 * V _{cr}	0.10			
17L180 17L* 17LV _{cr}	180 * V _{cr}	0.52 (FULL)	136 psl	@ ≈ 39600 lbs F.P. LOAD, ADJUST LOAD	
18L190 18L* 18LV _{cr}	190 * V _{cr}	0.30		FOR F.W. CURVA- TURE	
19L200 19L* 19LV _{cr}	200 * V _{cr}	0.10	; ; ;		

Continue to increase the test speed in increments of 5 or 10 mph in subsequent test cycles until the critical speed (V_{cr}) is reached.

(1) F.P. - flat plate, F.W. - flywheel

(2) The second character in the test cycle number identifies the method taken to compensate for flywheel curvature, either by pressure ("P") increase or by load ("L") reduction.

(3) All approximations (≈) were obtained from load-deflection cur.es, Goodyear report QTR 461B-2049-TL, 49x17/26PR

TABLE A-1. (CONTINUED)

TEST CYCLE NR.	TEST VEL. (mph)	GROOVE DEPTH (Inches)	INFLATION PRESSURE (psl)	NORMAL LOAD (lbs)	TEST DEFL.
20P190 20P* 20P <i>V_{cr}</i>	190 * V _{cr}	0.52 (FULL)	136 pst (F.P.) ADJUST PRESS FOR F.W.	≈ 21000 lbs © 136 psl F.P. & 20% DEFL	20% DEFL (≈ 2.52 INCHES)
21P210 21P* 21PV _{cr}	210 * V _{cr}	0.30	CURVA- TURE		
22P220 22P* 22PV _{cr}	220 * V _{cr}	0.10			
23P200 23P* 23PV _{cr}	200 * V _{cr}	0.52 (FULL)		≈9000 lbs @ 136 psl F.P. & 10% DEFL	10% DEFL (≈ 1.26 INCHES)
24P210 24P* 24PV _{cr}	210 * V _{cr}	0.30			
25P220 25P* 25PV _{cr}	220 * V _{cr}	0.10			

Continue to increase the test speed in increments of 5 or 10 mph in subsequent test cycles until the critical speed (V_{cr}) is reached.

(1) F.P. - flat plate, F.W. - flywheel

(2) The second character in the test cycle number identifies the method taken to compensate for flywheel curvature, either

by pressure ("P") increase or by load ("L") reduction.

(3) All approximations (≈) were obtained from load-deflection curves, Goodyear report QTR 461B-2049-TL, 49x17/26PR

TABLE A-1. (CONTINUED)

TEST CYCLE NR.	TEST VEL. (mph)	GROOVE DEPTH (Inches)	INFLATION PRESSURE (psl)	NORMAL LOAD (lbs)	TEST DEFL.
20L190 20L* 20LV _{cr}	190 * V _{cr}	0.52 (FULL)	136 psi	≈ 21000 lbs F.P. LOAD, ADJUST LOAD	20% DEFL (≈ 2.52 INCHES)
21L200 21L* 21LV _{cr}	200 * V _{cr}	0.30		FOR F.W. CURVA- TURE	
22L210 22L* 22LV _{cr}	210 * V _{cr}	0.10			
23L190 23L* 23LV _{cr}	190 * V _{cr}	0.52 (FULL)		≈ 9000 lbs F.P. LOAD, ADJUST LOAD	10% DEFL (≈ 1.26 INCHES)
24L200 24L* 24LV _{cr}	200 * V _{cr}	0.30		FOR F.W. CURVA- TURE	
25L210 25L* 25LV _{cr}	210 * V _{cr}	0.10			

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Continue to increase the test speed in increments of 5 or 10 mph in subsequent test cycles until the critical speed (V_{cr}) is reached.

(1) F.P. - flat plate, F.W. - flywheel
(2) The second character in the test cycle number identifies the method taken to compensate for flywheel curvature, either by pressure ("P") increase or by load ("L") reduction.
(3) All approximations (≈) were obtained from load-deflection curves, Goodyear report QTR 461B-2049-TL, 49x17/26PR

TABLE A-1. (CONTINUED)

TEST CYCLE NR.	TEST VEL. (mph)	GROOVE DEPTH (Inches)	INFLATION PRESSURE (ps1)	NORMAL LOAD (lbs)	TEST DEFL.
26P170 26P* 26PV _{cr}	170 * V _{cr}	0.52 (FULL)	102 psl (F.P.), ADJUST PRESS	≈ 17000 lbs © 102 psi F.P. & 20% DEFL	20% DEFL (≈ 2.52 INCHES)
27P180 27P* 27PV _{cr}	180 * V _{cr}	0.30	FOR F.W. CURVA- TURE		
28P190 28P* 28PV _{cr}	190 * V _{cr}	0.10			
29P180 29P* 29PV _{cr}	180 * V _{cr}	0.52 (FULL)		≈ 8000 lbs © 136 psl F.P. & 10% DEFL	10% DEFL (≈ 1.26 INCHES)
30P190 30P* 30PV _{cr}	190 * V _{cr}	0.30			
31P200 31P* 31PV _{cr}	200 * V _{cr}	0.10			

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NOTES:

Continue to increase the test speed in increments of 5 or 10 mph in subsequent test cycles until the critical speed $\{V_{cr}\}$ is reached.

(1) F.P. - flat plate, F.W. - flywheel

(2) The second character in the test cycle number identifies the method taken to compensate for flywheel curvature, either by pressure ("P") increase or by load ("L") reduction.

(3) All approximations (≈) were obtained from load-deflection curves, Goodyear report QTR 461B-2049-TL, 49x17/26PR

TABLE A-1. (CONTINUED)

TEST CYCLE NR.	TEST VEL. (mph)	GROOVE DEPTH (Inches)	INFLATION PRESSURE (ps1)	NORMAL LOAD (lbs)	TEST DEFL.
26L160 26L* 26LV _{cr}	160 * V _{cr}	0.52 (FULL)	102 psl	≈ 17000 lbs F.P. LOAD, ADJUST LOAD	20% DEFL (≈ 2.52 INCHES)
27L170 27L* 27LV _{cr}	170 * V _{cr}	0.30		FOR F.W. CURVA- TURE	
28L180 28L* 28LV _{cr}	180 * V _{cr}	0.10			
29L160 29L* 29LV _{cr}	160 * V _{cr}	0.52 (FULL)		≈ 8000 lbs F.P. LOAD, ADJUST LOAD	10% DEFL (≈ 1.26 INCHES)
30L170 30L* 30LV _{cr}	170 * V _{cr}	0.30		FOR F.W. CURVA- TURE	
31L180 31L* 31LV _{cr}	180 * V _{cr}	0.10			

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Continue to increase the test speed in increments of 5 or 10 mph in subsequent test cycles until the critical speed (V_{cr}) is

(1) F.P. - flat plate, F.W. - flywheel
(2) The second character in the test cycle number identifies the method taken to compensate for flywheel curvature, either by pressure ("P") increase or by load ("L") reduction.

(3) All approximations (≈) were obtained from load-deflection curves, Goodyear report QTR 461B-2049-TL, 49x17/26PR

ABBREVIATIONS, ACRONYMS, and SYMBOLS

Distance taken normal to the tire plane centerline from a centerline to point of application of force Q Tire aspect ratio A_R Empirical load/deflection constant Tire vertical deflection d d_r Tire rated vertical deflection Tire outside diameter D_{o} Radial growth due to centrifugal effects dhdmDifferential mass element per unit width of tread \boldsymbol{E} Modulus of elasticity E_f Fabric modulus of elasticity Rubber-tread modulus of elasticity E_r EIBending stiffness of tread band treated as a beam F_{c} Carcass force F_z Vertical load **Gravity constant** g h Tire section height Foundation spring rate of the tread band k K_z Tire vertical stiffness, slope of the vertical load/deflection curve l Cord length \boldsymbol{L} Length of beam Total tire mass m_t Tire inflation pressure p_i Tire rated inflation pressure p_r Centrifugal force equivalent to half the total centrifugal \boldsymbol{Q} force acting on the tire cross-section Tire rolling radius r_o time or average thickness of tread and carcass at the tire crown TTension force in tread band Thickness of the cord-rubber fabric region Thickness of the rubber-tread region t_r \boldsymbol{U} Internal potential energy U_{ef} Internal energy due to the elastic foundation U_{se} Strain energy wave speed υ VExternal potential energy V_{cr} Critical speed External potential energy due to distributed loads V_d V_t External potential energy due to tension Vertical beam deflection

 W_t

 w_s

Total tire weight Cross-sectional width

Longitudinal distance along the beam axis

- z Radial tire distance from cross-section centroid
- δ First-order variation
- δW_e Virtual work performed by external forces
- δW_i Virtual work performed by internal forces
- σ_{xx} Longitudinal stress
- γ Cord half angle
- ρ Tread density
- ρ_1 Mass per unit area of tire surface
- $\rho^{\bar{I}}$ Effective tread density
- ρ_m Average tread mass density
- ϵ_{xx} Longitudinal strain
- ω Tire rotational speed

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